

Name: \_\_\_\_\_

Please show all work and explain your answers.

1. Expand  $(z - i)^{-1} + (z - 2)^{-1}$  in a Laurent series centered at the origin and valid in the annulus  $\{z : 1 < |z| < 2\}$ .
2. Integrate  $\cot z$  around the unit circle.
3. Use Rouché's theorem to determine the number of zeros, counted with multiplicity, of  $z^3 - 5z + 1$  outside the unit disc.
4. Find a fractional linear transformation that maps the unit disc to the right half-plane.

1	2	3	4	total (40)	%

Prelim. course grade: %