Name: _____

Please show all work and explain your answers.

- 1. Integrate $\frac{\cos z \, dz}{z(z^2+4)}$ around the circle of radius 2 centered at -i.
- 2. Integrate $\frac{e^{z^2} dz}{z^3}$ around the same circle as above.
- 3. Integrate \overline{z} along the straight line segment from 1 to *i*.
- 4. Suppose $f: \mathbb{C} \to \mathbb{C}$ is entire and the real part $\Re[f(z)] > 0$ for all $z \in \mathbb{C}$. What can you conclude about f? Prove your assertion. Cite any theorems you use in your proof.

1	2	3	4	total (40)	%

Prelim. course grade: %