Name: $\qquad$

Please show all work and explain your answers.

1. Integrate $\frac{\cos z d z}{z\left(z^{2}+4\right)}$ around the circle of radius 2 centered at $-i$.
2. Integrate $\frac{e^{z^{2}} d z}{z^{3}}$ around the same circle as above.
3. Integrate $\bar{z}$ along the straight line segment from 1 to $i$.
4. Suppose $f: \mathbf{C} \rightarrow \mathbf{C}$ is entire and the real part $\mathfrak{R}[f(z)]>0$ for all $z \in \mathbf{C}$. What can you conclude about $f$ ? Prove your assertion. Cite any theorems you use in your proof.

| 1 | 2 | 3 | 4 | total (40) | $\%$ |
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| Prelim. course grade: |  |  |  |  | $\%$ |

