Name: $\qquad$

1. Let $z_{1}=1+i$ and $z_{2}=2 e^{i 2 \pi / 3}$. Sketch $z_{1}+z_{2}$ and $z_{2} / \overline{z_{1}}$.
2. When considered as a plane transformation, $f(z)$ has the effect of dilating by 3, rotating by $\pi / 3$, followed by an upward shift by 3 . Find a formula for $f(z)$.
3. Let $f(x+i y)=x^{2}+y^{2}+2 i x y$. Determine where $f$ is complex differentiable.
4. Parametrize the lower half circle of radius 1 centered at $i$ from $i-1$ to $i+1$ and integrate $y d x-x d y$ along this path.
5. Integrate $x y^{2}$ over the solid triangle with vertices $0,2, i$.

| 1 | 2 | 3 | 4 | 5 | total (50) | $\%$ |
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| Prelim. course grade: $\%$ |  |  |  |  |  |  |

