Name: $\qquad$
Please show all work and justify your answers. Supply brief narration with your solutions and draw conclusions.

1. Find a parametrization for the line of intersection of the planes $x+2 y+3 z=6$ and $x-y=0$. Sketch.
2. The curves $t \widehat{\imath}+t^{2} \widehat{\jmath}+t^{3} \widehat{k}$ and $\sin (t) \widehat{\imath}+\sin (2 t) \widehat{\jmath}+t \widehat{k}$ intersect at the origin. Find the angle of intersection.
3. Find the limit of $x y^{3} /\left(x^{4}+2 y^{4}\right)$ as $(x, y) \rightarrow(0,0)$ or show that the limit fails to exist.
4. Suppose $f$ is a differentiable function of $x$ and $y$ and $g(u, v)=f\left(e^{u}+\sin v, e^{u}+\cos v\right)$. Use the table of values to find the directional derivative of $g$ at the origin along the main diagonal.

| $(x, y)$ | $f$ | $g$ | $f_{x}$ | $f_{y}$ |
| :---: | :---: | :---: | :---: | :---: |
| $(0,0)$ | 2 | 3 | 4 | 5 |
| $(1,2)$ | 6 | 7 | 8 | 9 |

5. Integrate $x /(1+x y)$ over the unit square $[0,1] \times[0,1]$.

| 1 | 2 | 3 | 4 | 5 | total (50) | $\%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |
| Prelim. course grade: |  |  |  |  |  | $\%$ |

