Name: $\qquad$
Please show all work and justify your answers. Supply brief narration with your solutions and draw conclusions.

1. Evaluate the following infinite sums
(a) $0.6+0.36+0.216+0.1296+0.07776+\ldots$
(b) $\sum_{n=2}^{\infty} \frac{1}{n^{2}-1}$
2. Determine whether the following series converge
(a) $\frac{1}{2 \ln 2}+\frac{1}{3 \ln 3}+\frac{1}{4 \ln 4}+\ldots$
(b) $\sum_{n=1}^{\infty} \frac{5+2 n}{\left(1+n^{2}\right)^{2}}$
3. Find a power series representation for $\frac{1}{4+x^{2}}$ and determine its interval of convergence.
4. Find two unit vectors in the plane whose angle with $u=[5,4]$ is $\pi / 6$. Sketch.
5. Given three points $A=[0,-2,0], B=[4,1,-2]$, and $C=[5,3,1]$ find the area of the triangle having these points as vertices. Also find a unit vector perpendicular to the plane containing these points. Sketch.

| 1 | 2 | 3 | 4 | 5 | total (50) | $\%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
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| Prelim. course grade: |  |  |  |  |  | $\%$ |

