Name: $\qquad$
Please show all work and justify your statements. Label sketches, draw conclusions (using complete sentences and including units), and box your final answers as appropriate.

1. Find a plane that intersects the graph of $z=\left(x^{2}+1\right) \sin y+x y^{2}$ in a parabola. Repeat the question for a straight line.
Hint: in each case set one variable constant.
2. Determine whether $\frac{x y}{x^{2}+y^{2}}$ has a limit as $(x, y) \rightarrow(0,0)$.

If yes, what is the limit? If no, explain why the limit fails to exist.
3. H.M.S. Jabanic encounters a $5 \mathrm{~km} / \mathrm{h}$ current towards $30^{\circ}$ south of east. If the engines can produce a maximum speed of $15 \mathrm{~km} / \mathrm{h}$ in still water, what is the fastest progress Jabanic can make due west?
4. What is the angle between the planes $2 x-3 y+4 z=2$ and $x+y-3 z=5$ ? What is the direction of the intersection of these planes?
5. Find the local linearization of $x \sin (y \ln x)$ at the point $(2,1)$.

| 1 | 2 | 3 | 4 | 5 | total (50) | $\%$ |
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| Prelim. course grade: |  |  |  |  |  |  |

