Calculus II / MAT 1223
Midterm 1 / October 21, 1999 / Instructor: D. Gokhman

Name:
Please show all work and box the answers, where appropriate.

1. (15 pts.) Evaluate
(a) $\int \frac{\left(z^{2}+1\right)^{2}}{\sqrt{z^{3}}} d z$
(b) $\int \frac{(\sqrt{t}+1)^{8}}{\sqrt{t}} d t$
(c) $\frac{d}{d x} \int_{\sqrt{x}}^{1} \cos ^{8}(t) d t$
2. (10 pts.) Find the volume of the solid of revolution generated by rotating the region bounded by $y-\sqrt{x}=0, x=4, y=0$ around the $y$ axis.
3. ( 10 pts .) Find the surface area generated by rotating the curve $x=3 t, y=t^{2}-1$, $0 \leq t \leq 1$ around the $y$ axis.
4. ( 20 pts.) Find the centroid of the region between the curves $y=1-x^{2}$ and $y=x-1$. Sketch the region and the centroid.

| 1 | 2 | 3 | 4 | total (55) | $\%$ |
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