Midterm 1 / 2014.2.21 / CS 3333.001 / Mathematical foundations of computer science

## Name: \_

Please show all work and justify your answers.

- 1. Expand decimal 151 in binary, octal and hexadecimal. What is the decimal expansion of hexadecimal BAD?
- 2. Apply Euclid's algorithm to 74 and 35 to show that they are co-prime. Find the Bézout coefficients.
- 3. Use the Chinese remainder theorem to solve the following system of congruences:

 $x \equiv 2 \mod 4$ ,  $2x \equiv 3 \mod 5$ ,  $x \equiv 1 \mod 9$ .

- 4. For which  $n \ge 0$  is  $4^n < n!$ ? Prove your assertion.
- 5. What amounts can be obtained with only \$5 and \$2 bills? Prove your assertion.

1	2	3	4	5	total (50)	%